

# Anti-triplet Charmed Baryon Weak Decays with SU(3) Flavor Symmetry

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## Motivation

- Unknown baryon wave functions
- Failure of the conventional factorization approach

$$\mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \pi^0)_{EXP} = (1.24 \pm 0.10)\%$$

- Measurements with higher precision in Belle and BESSIII

$$\mathcal{B}(\Lambda_c^+ \rightarrow p K^- \pi^+) = (6.23 \pm 0.33)\%$$

- C. Q. Geng, Y. K. Hsiao, C. W. Liu and T. H. Tsai, JHEP **1711**, 147 (2017)
- C. Q. Geng, Y. K. Hsiao, C. W. Liu and T. H. Tsai, Eur. Phys. J. C **78**, 593 (2018)
- C. Q. Geng, Y. K. Hsiao, C. W. Liu and T. H. Tsai, Phys. Rev. D **97**, 073006 (2018)
- C. Q. Geng, Y. K. Hsiao, C. W. Liu and T. H. Tsai, arXiv:1810.01079 [hep-ph].

# Outline

- 1 Introduction of SU(3) Flavor Symmetry
- 2 Anti-triplet Charmed Baryon Weak Decays
- 3 Numerical Results

# Introduction of SU(3) Flavor Symmetry

$$\begin{aligned}|_1\rangle &= |u\rangle, |_2\rangle = |d\rangle, |_3\rangle = |s\rangle \\|{}^1\rangle &= |\bar{u}\rangle, |{}^2\rangle = |\bar{d}\rangle, |{}^3\rangle = |\bar{s}\rangle\end{aligned}$$

$$\begin{aligned}\pi^+ &= |{}_1^2\rangle = \delta_{i2} \delta^{j1} |{}_j^i\rangle = (\pi^+)_i^j |{}_j^i\rangle \\M &= (M)_i^j |{}_j^i\rangle\end{aligned}$$

$$(M)_i^j = \begin{pmatrix} \frac{1}{\sqrt{2}}(\pi^0 + c\phi\eta + s\phi\eta') & \pi^- & K^- \\ \pi^+ & \frac{-1}{\sqrt{2}}(\pi^0 - c\phi\eta - s\phi\eta') & \bar{K}^0 \\ K^+ & K^0 & -s\phi\eta + c\phi\eta' \end{pmatrix}_{ij},$$

where  $(c\phi, s\phi) = (\cos \phi, \sin \phi)$  and  $\phi = (39.3 \pm 1.0)^\circ$ .<sup>1</sup>

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<sup>1</sup>T. Feldmann, P. Kroll and B. Stech, Phys. Rev. D **58**, 114006 (1998); Phys. Lett. B **449**, 339 (1999).

# Introduction of SU(3) Flavor Symmetry

## Invariant tensor

$$\epsilon^{ijk}|ijk\rangle$$

$$\delta_j^i|j_i\rangle$$

# Introduction of SU(3) Flavor Symmetry

## Invariant tensor

$$\epsilon^{ijk} |ijk\rangle \quad \delta_j^i |j_i\rangle$$

Antisymmetric tensor gives us singlet

$$\frac{1}{\sqrt{2}} (| \uparrow\downarrow \rangle - | \downarrow\uparrow \rangle) ,$$

$$\frac{1}{\sqrt{6}} (|rgb\rangle - |rbg\rangle + |gb\color{red}r\rangle - |\color{green}grb\rangle + |\color{blue}brg\rangle - |\color{blue}bgr\rangle)$$

Same thing happens in color states of mesons

$$\frac{1}{\sqrt{3}} (|r\bar{r}\rangle + |g\bar{g}\rangle + |b\bar{b}\rangle)$$

# Introduction of SU(3) Flavor Symmetry

Singly charmed baryons

$$\Lambda_c^+ = |udc\rangle - |duc\rangle = |12\rangle_{B_c} - |21\rangle_{B_c} = \epsilon^{ijk} \delta_{k3} |ij\rangle_{B_c}$$

$$(\mathbf{B}_c)_i = (\Xi_c^0, -\Xi_c^+, \Lambda_c^+)_i$$

Octet Baryons

$$\mathbf{B} = \mathbf{B}^{ijk} |ijk\rangle = (\mathbf{B}_n)_i^j \epsilon^{ljk} |ijk\rangle$$

$$p = |112\rangle - |121\rangle = (\delta^{i1}\delta^{j1}\delta^{k2} - \delta^{i1}\delta^{j2}\delta^{k1}) |ijk\rangle = (\delta^{i1}\delta_{l3} \epsilon^{ljk}) |ijk\rangle$$

$$(\mathbf{B}_n)_j^i = \begin{pmatrix} \frac{1}{\sqrt{6}}\Lambda + \frac{1}{\sqrt{2}}\Sigma^0 & \Sigma^+ & p \\ \Sigma^- & \frac{1}{\sqrt{6}}\Lambda - \frac{1}{\sqrt{2}}\Sigma^0 & n \\ \Xi^- & \Xi^0 & -\sqrt{\frac{2}{3}}\Lambda \end{pmatrix}_{ij}$$

# Charmed Baryon Weak Decays

Effective Hamiltonian for c transition

$$\mathcal{H}_{\text{eff}} = \frac{G_F}{\sqrt{2}} (c_+ O_+ + c_- O_-) .$$

$$O_+ = \frac{1}{2} \sum_{q,q'=d,s} V_{uq} V_{cq'}^* ((\bar{u}q)(\bar{q}'c) + (\bar{q}'q)(\bar{u}c)) ,$$

$$O_- = \frac{1}{2} \sum_{q,q'=d,s} V_{uq} V_{cq'}^* ((\bar{u}q)(\bar{q}'c) - (\bar{q}'q)(\bar{u}c)) ,$$

where  $(\bar{q}q') \equiv \bar{q}^\alpha \gamma_\mu (1 - \gamma_5) q_\alpha$ .

# Charmed Baryon Weak Decays

Effective Hamiltonian for c transition

$$\mathcal{H}_{\text{eff}} = \frac{G_F}{2\sqrt{2}} \left( c_- H(6)_{lk} (\epsilon^{ijl}/2) O_{ij}^k + c_+ H(\bar{15})_k^{ij} O_{ij}^k \right)$$

$$O_{ij}^k = (\bar{q}_i q_k)_{V-A} (\bar{q}_j c)_{V-A} \quad s_c \equiv V_{us}$$

$$H(6)_{ij} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 2 & -2s_c \\ 0 & -2s_c & 2s_c^2 \end{pmatrix}_{ij},$$

$$H(\bar{15})_k^{ij} = \left( \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}_{ij}, \begin{pmatrix} 0 & s_c & 1 \\ s_c & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix}_{ij}, \begin{pmatrix} 0 & -s_c^2 & -s_c \\ -s_c^2 & 0 & 0 \\ -s_c & 0 & 0 \end{pmatrix}_{ij} \right)_k$$

# Charmed Baryon Weak Decays

$$\begin{aligned}\mathcal{A}(I \rightarrow F) &= \langle I | \mathcal{H}_{\text{eff}} | F \rangle = \frac{G_F}{\sqrt{2}} T(\mathbf{B}_c \rightarrow \mathbf{B}_n M) \\ &= (\mathbf{B}_n)_j^i M_m^k H_p^{no} (\mathbf{B}_c)_q \langle (j)_n (m)_M | O_{no}^p | q \rangle_{\mathbf{B}_c}\end{aligned}$$

The process  $B_c \rightarrow B_n M$  with  $T^{ij} \equiv (\mathbf{B}_c)_k \epsilon^{ijk}$

$$\begin{aligned}T(\mathcal{O}_6) &= a_1 H(6)_{ij} T^{ik} (\mathbf{B}_n)_k^l (M)_l^j + a_2 H(6)_{ij} T^{ik} (M)_k^l (\mathbf{B}_n)_l^j \\ &\quad + a_3 H(6)_{ij} (\mathbf{B}_n)_k^i (M)_l^j T^{kl} + h H(6)_{ij} T^{ik} (\mathbf{B}_n)_k^j (M)_l^l, \\ T(\mathcal{O}_{\overline{15}}) &= a_4 H(\overline{15})_k^l (\mathbf{B}_c)_j (M)_i^j (\mathbf{B}_n)_l^k + a_5 (\mathbf{B}_n)_j^l (M)_i^l H(\overline{15})_l^{jk} (\mathbf{B}_c)_k \\ &\quad + a_6 (\mathbf{B}_n)_l^k (M)_j^i H(\overline{15})_i^{jl} (\mathbf{B}_c)_k + a_7 (\mathbf{B}_n)_i^l (M)_j^i H(\overline{15})_l^{jk} (\mathbf{B}_c)_k \\ &\quad + h' H(\overline{15})_i^{jk} (\mathbf{B}_n)_k^l (M)_l^j (\mathbf{B}_c)_j,\end{aligned}$$

## Example

$$\mathcal{A}(\Lambda_c^+ \rightarrow \Sigma^+ \pi^0) = \sqrt{2} \left( a_1 - a_2 - a_3 - \frac{a_5 - a_7}{2} \right)$$

# Charmed Baryon Weak Decays

$$\begin{aligned} T(\mathcal{O}_6) &= a_1 H(6)_{ij} T^{ik} (\mathbf{B}_n)_k^l (M)_l^j + a_2 H(6)_{ij} T^{ik} (M)_k^l (\mathbf{B}_n)_l^j \\ &+ a_3 H(6)_{ij} (\mathbf{B}_n)_k^l (M)_l^j T^{kl} + h H(6)_{ij} T^{ik} (\mathbf{B}_n)_k^l (M)_l^j, \\ T(\mathcal{O}_{\overline{15}}) &= a_4 H(\overline{15})_k^l (\mathbf{B}_c)_j (M)_i^j (\mathbf{B}_n)_l^k + a_5 (\mathbf{B}_n)_j^l (M)_i^l H(\overline{15})_l^{jk} (\mathbf{B}_c)_k \\ &+ a_6 (\mathbf{B}_n)_l^k (M)_j^i H(\overline{15})_i^{jl} (\mathbf{B}_c)_k + a_7 (\mathbf{B}_n)_i^l (M)_j^i H(\overline{15})_l^{jk} (\mathbf{B}_c)_k \\ &+ h' H(\overline{15})_i^{jk} (\mathbf{B}_n)_k^l (M)_l^j (\mathbf{B}_c)_j, \end{aligned}$$

$\Lambda_c^+$	Transition Amplitude
$\Sigma^0 \pi^+$	$-\sqrt{2}(a_1 - a_2 - a_3 - \frac{a_5 - a_7}{2})$
$\Sigma^+ \pi^0$	$\sqrt{2}(a_1 - a_2 - a_3 - \frac{a_5 - a_7}{2})$
$\Sigma^+ \eta$	$\sqrt{2}c\phi(-a_1 - a_2 + a_3 - 2h + \frac{a_5 + a_7 + 2h'}{2}) + s\phi(-a_4 + 2h - h')$
$\Sigma^+ \eta'$	$\frac{\sqrt{2}s\phi}{2}(-a_1 - a_2 + a_3 - 2h + \frac{a_5 + a_7 + 2h'}{2}) - c\phi(-a_4 + 2h - h')$
$\Xi^0 K^+$	$-2(a_2 - \frac{a_4 + a_7}{2})$
$p \bar{K}^0$	$-2(a_1 - \frac{a_5 + a_6}{2})$
$\Lambda^0 \pi^+$	$-\sqrt{\frac{2}{3}}(a_1 + a_2 + a_3 - \frac{a_5 - 2a_6 + a_7}{2})$

# Charmed Baryon Weak Decays

Table: The  $T$ -amps of the  $\mathbf{B}_c \rightarrow \mathbf{B}_n M$  decays.

$\Xi^0$	$T$ -amp	$\Xi^+$	$T$ -amp	$\Lambda^0$	$T$ -amp
$\Sigma^+ K^-$	$2(a_2 + \frac{a_1 - a_3}{2})$ - $\sqrt{2}(a_2 + a_3 - \frac{a_1 - a_3}{2})$	$\Sigma^+ K^0$	$-2(a_3 - \frac{a_1 - a_3}{2})$ $\Xi^0 \pi^+$	$\Sigma^0 \pi^+$	$-\sqrt{2}(a_1 - a_2 - a_3 - \frac{a_1 - a_3}{2})$ + $\sqrt{2}(a_1 - a_2 - a_3 - \frac{a_1 - a_3}{2})$
$\Xi^0 \bar{K}^0$	$-\sqrt{2}(a_2 + a_3 - \frac{a_1 - a_3}{2})$	$\Xi^0 \pi^0$	$2(a_3 + \frac{a_1 - a_3}{2})$	$\Sigma^+ \eta$	$\sqrt{2}(a_1 - a_2 - a_3 - \frac{a_1 - a_3}{2})$ + $\sqrt{2}c\phi(-a_1 - a_2 + a_3 - 2h + \frac{a_1 - a_3 - 2h'}{2})$
$\Xi^0 \pi^0$	$-\sqrt{2}(a_1 - a_2 - \frac{a_1 - a_3}{2})$	$\Xi^0 \eta$	$\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 + 2h'}{2})$ - $2c\phi(a_2 + h + \frac{a_1 - a' - 2h'}{2})$	$\Sigma^+ \eta'$	$+ \sqrt{2}d\phi(-a_1 - a_2 + a_3 - 2h + \frac{a_1 - a_3 + 2h'}{2})$ - $c\phi(-a_1 - 2h - h')$
$\Xi^0 \eta$	$\sqrt{2}x\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 + 2h'}{2})$ + $c\phi(a_2 + h + \frac{a_1 - a' - 2h'}{2})$	$\Xi^0 \eta'$	$-2(a_2 - \frac{a_1 - a_3}{2})$ $\Xi^0 K^+$	$\Xi^0 K^+$	$-2(a_2 - \frac{a_1 - a_3}{2})$
$\Xi^0 \eta'$	$\sqrt{2}x\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 + 2h'}{2})$ + $\sqrt{2}c\phi(a_2 + h + \frac{a_1 - a' - 2h'}{2})$	$\mu K^0$	$-2(a_1 + a_2 + a_3 - \frac{a_1 - a_3}{2})$	$\mu K^0$	$-2(a_1 + a_2 + a_3 - \frac{a_1 - a_3}{2})$
$\Xi^- \pi^+$	$2(a_2 + \frac{a_1 - a_3}{2})$ - $\sqrt{\frac{1}{3}}(2a_1 - a_2 - a_3 + \frac{2a_1 - a_2 - a_3}{2})$	$\Xi^- \pi^+$	$\sqrt{\frac{1}{3}}(a_1 + a_2 + a_3 - \frac{a_1 - a_3}{2})$	$\mu \eta$	$\sqrt{\frac{1}{3}}(a_1 + a_2 + a_3 - \frac{a_1 - a_3}{2})$
$\Xi^- \pi^-$	$-2(a_2 + \frac{a_1 - a_3}{2})$	$\Sigma^+ \pi^0$	$\sqrt{2}(a_1 - a_2 + \frac{a_1 - a_3}{2})z_c$	$\Sigma^+ \eta$	$-2(a_1 - a_2 - a_3 - \frac{a_1 - a_3}{2})z_c$
$\Sigma^- \pi^+$	$-2(a_2 + \frac{a_1 - a_3}{2})z_c$	$\Sigma^+ \eta$	$-\sqrt{2}(a_1 - a_2 - \frac{a_1 - a_3}{2})z_c$	$\Sigma^+ \eta'$	$-\sqrt{2}(a_1 - a_2 - a_3 - \frac{a_1 - a_3}{2})z_c$
$\Sigma^0 \pi^0$	$-(a_2 + a_3 - \frac{a_1 - a_3 - a_2 - a_3}{2})z_c$	$\Sigma^- \eta$	$[\sqrt{2}c\phi(a_1 + a_2 + 2h - \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $\sqrt{2}x\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})$ - $2\sqrt{2}c\phi(a_1 + a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})z_c$	$\Sigma^- \eta'$	$[\sqrt{2}c\phi(a_1 + a_2 + 2h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$
$\Xi^0 \eta$	$-(a_2 + a_3 - \frac{a_1 - a_3 - a_2 - a_3}{2})z_c$	$\Sigma^0 \eta$	$[\sqrt{2}c\phi(a_1 + a_2 + 2h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$ + $\sqrt{2}x\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$	$\Xi^0 \eta'$	$[\sqrt{2}c\phi(a_1 + a_2 + 2h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$
$\Sigma^0 \eta'$	$-(a_2 + a_3 - \frac{a_1 - a_3 - a_2 - a_3}{2})z_c$	$\Xi^0 \eta'$	$[\sqrt{2}c\phi(a_1 + a_2 + 2h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$ + $\sqrt{2}x\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$	$\Xi^0 K^+$	$-2(a_1 - a_2 - a_3 - \frac{a_1 - a_3}{2})z_c$
$\Xi^- K^+$	$2(a_2 + \frac{a_1 - a_3}{2})z_c$	$\Xi^0 K^+$	$-\sqrt{2}(a_1 - a_2 - a_3 - \frac{a_1 - a_3}{2})z_c$	$\mu \eta^0$	$-\sqrt{2}(a_1 - a_2 - a_3 - \frac{a_1 - a_3}{2})z_c$
$\Xi^- K^-$	$2(a_2 + \frac{a_1 - a_3}{2})z_c$	$\mu \eta^0$	$-\sqrt{2}(a_2 + a_3 - \frac{a_1 - a_3}{2})z_c$	$\mu \eta$	$-\sqrt{2}(a_2 + a_3 - \frac{a_1 - a_3}{2})z_c$
$\Xi^0 K^0$	$2(a_1 - a_2 - a_3 + \frac{a_1 - a_3}{2})z_c$	$\mu \eta$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$	$\mu \eta'$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$
$n K^0$	$-2(a_1 - a_2 - a_3 + \frac{a_1 - a_3}{2})z_c$	$\mu \eta'$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$	$\Xi^0 \pi^0$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$
$\Lambda^0 \pi^0$	$\sqrt{\frac{1}{3}}(a_1 + a_2 - 2a_3)$ + $\frac{a_1 - a_2 - a_3 - 2a_1}{2}z_c$	$\Xi^0 \pi^0$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$	$\Xi^0 \pi^0$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$
$\Lambda^0 \eta$	$[\frac{\sqrt{2}c\phi}{2}(a_1 + a_2 - 2a_3 + 6h + \frac{a_1 - a_2 - a_3 - 2a_1}{2})z_c$ + $\frac{\sqrt{2}x\phi}{2}(2a_1 + 2a_2 - a_3 + 3h + \frac{a_1 - a_2 - a_3 - 2a_1}{2})z_c$	$\Xi^0 \eta$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$	$\Xi^0 \eta$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$
$\Lambda^0 \eta'$	$[\frac{\sqrt{2}c\phi}{2}(a_1 + a_2 - 2a_3 + 6h + \frac{a_1 - a_2 - a_3 - 2a_1}{2})z_c$ + $\frac{\sqrt{2}x\phi}{2}(2a_1 + 2a_2 - a_3 + 3h + \frac{a_1 - a_2 - a_3 - 2a_1}{2})z_c$	$\Xi^0 \eta'$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$	$\Xi^0 K^+$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$
$\Xi^- K^-$	$-2(a_2 + \frac{a_1 - a_3}{2})z_c$	$\Xi^0 K^0$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$	$\mu \eta^0$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$
$\Sigma^- K^+$	$-2(a_2 + \frac{a_1 - a_3}{2})z_c$	$\mu \eta^0$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$	$\mu \eta$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$
$\Sigma^0 K^0$	$\sqrt{2}(a_1 + a_2 - 2a_3)$ + $\frac{a_1 - a_2 - a_3 - 2a_1}{2}z_c$	$\mu \eta$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$	$\Xi^0 \pi^0$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$
$n \pi^0$	$\sqrt{2}(a_1 + a_2 - 2a_3)$ + $\frac{a_1 - a_2 - a_3 - 2a_1}{2}z_c$	$\mu \eta'$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$	$\Xi^0 \pi^0$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$
$n \eta$	$[-\sqrt{2}c\phi(a_2 - 2h + \frac{a_1 - a_2 - a_3}{2})z_c^2$ + $2\sqrt{2}c\phi(a_1 - a_2 + h + \frac{a_1 - a_2 - a_3}{2})z_c^2$	$\Xi^0 \eta$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$	$\Xi^0 \pi^+$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$
$n \eta'$	$[-\sqrt{2}c\phi(a_2 - 2h + \frac{a_1 - a_2 - a_3}{2})z_c^2$ + $\sqrt{2}x\phi(a_1 - a_2 - 2h + \frac{a_1 - a_2 - a_3}{2})z_c^2$	$\Xi^0 \eta'$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$	$\Xi^0 K^+$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$
$A^0 K^0$	$-\sqrt{2}(a_1 - a_2 - a_3 + \frac{a_1 - a_2 - a_3}{2})z_c^2$ - $\sqrt{\frac{1}{3}}(a_1 - 2a_2 - 2a_3 + \frac{a_1 - a_2 - a_3 - 2a_1}{3})z_c^2$	$\Xi^0 K^0$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$	$\Xi^0 K^0$	$[\sqrt{2}c\phi(a_1 - a_2 + 2h + \frac{a_1 - a_3 - a_2 - a_3 + 2h'}{2})$ + $2\sqrt{2}c\phi(a_2 - h - \frac{a_1 - a_3 - a_2 - a_3 - 2h'}{2})z_c$

# Charmed Baryon Weak Decays

We omit  $O_+$  for two reasons

- $\frac{c_+}{c_-} \approx 0.4$
- Baryon pole:  
 $\langle \mathbf{B}_i | O_+ | \mathbf{B}_p \rangle = 0$

H. Y. Cheng, X. W. Kang and F. Xu,

"Singly Cabibbo-suppressed hadronic decays of  $\Lambda_c^+$ ,"

Phys. Rev. D **97**, no. 7, 074028 (2018)

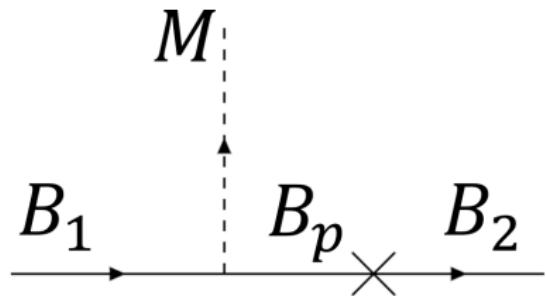


Figure: Baryon pole

# Numerical Results

## Fitting Results

$(a_1, a_2, a_3, h) = (0.244 \pm 0.006, 0.115 \pm 0.014, 0.088 \pm 0.019, 0.105 \pm 0.073) \text{ GeV}^3$ ,  
 $(\delta_{a_1}, \delta_{a_2}, \delta_{a_3}, \delta_h) = (0, 78.1 \pm 7.1, 35.1 \pm 8.7, 10.2 \pm 29.6)^\circ$ ,  
 $\chi^2/d.o.f = 5.32/3 = 1.77$ .

Table: The data of the  $\mathbf{B}_c \rightarrow \mathbf{B}_n M$  decays.

Branching ratios	Data	Branching ratios	Data
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow p \bar{K}^0)$	$3.16 \pm 0.16$	$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \eta)$	$0.70 \pm 0.23$
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Lambda \pi^+)$	$1.30 \pm 0.07$	$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow \Lambda K^+)$	$6.1 \pm 1.2$
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \pi^0)$	$1.24 \pm 0.10$	$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^0 K^+)$	$5.2 \pm 0.8$
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^0 \pi^+)$	$1.29 \pm 0.07$	$10^4 \mathcal{B}(\Lambda_c^+ \rightarrow p \eta)$	$12.4 \pm 3.0$
$10^2 \mathcal{B}(\Lambda_c^+ \rightarrow \Xi^0 K^+)$	$0.50 \pm 0.12$	$\mathcal{R} = \frac{\mathcal{B}(\Xi_c^0 \rightarrow \Lambda \bar{K}^0)}{\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+)}$	$0.420 \pm 0.056$

# Numerical Results

## Fitting Results

$(a_1, a_2, a_3, h) = (0.244 \pm 0.006, 0.115 \pm 0.014, 0.088 \pm 0.019, 0.105 \pm 0.073) \text{ GeV}^3$ ,  
 $(\delta_{a_1}, \delta_{a_2}, \delta_{a_3}, \delta_h) = (0, 78.1 \pm 7.1, 35.1 \pm 8.7, 10.2 \pm 29.6)^\circ$ ,  
 $\chi^2/d.o.f = 5.32/3 = 1.77$ .

Comparing with the experiment announcement in 2018 November

Decay branching ratio	$\mathcal{B}_{th}$	$\mathcal{B}_{ex}$
$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+)$	$(1.57 \pm 0.07)\%$	$(1.80 \pm 0.52)\%$ <sup>2</sup>
$\mathcal{B}(\Lambda_c^+ \rightarrow \Sigma^+ \eta')$	$(1.0^{+1.8}_{-0.8})\%$	$(1.34 \pm 0.57)\%$ <sup>3</sup>

<sup>2</sup> arXiv:1811.09738 [hep-ex]. "First measurements of absolute branching fractions of  $\Xi_c^0$  at Belle,"

<sup>3</sup> arXiv:1811.08028 [hep-ex]. "Evidence for the decays of  $\Lambda_c^+ \rightarrow \Sigma^+ \eta$  and  $\Sigma^+ \eta'$ ,"

# Numerical Results

**Table:** The numerical results of the  $B_c \rightarrow B_n M$

$\Xi_c^0$	our results	$\Xi_c^+$	our results	$\Lambda_c^+$	our results
$10^3 \mathcal{B}_{\Sigma^+ K^-}$	$3.5 \pm 0.9$	$10^3 \mathcal{B}_{\Sigma^+ \bar{K}^0}$	$8.0 \pm 3.9$	$10^3 \mathcal{B}_{\Sigma^0 \pi^+}$	$(1.3 \pm 0.2)^\dagger$
$10^3 \mathcal{B}_{\Sigma^0 \bar{K}^0}$	$4.7 \pm 1.2$	$10^3 \mathcal{B}_{\Xi^0 \pi^+}$	$8.1 \pm 4.0$	$10^3 \mathcal{B}_{\Sigma^+ \pi^0}$	$(1.3 \pm 0.2)^\dagger$
$10^3 \mathcal{B}_{\Xi^0 \pi^0}$	$4.3 \pm 0.9$			$10^2 \mathcal{B}_{\Sigma^+ \eta}$	$(0.7^{+0.4}_{-0.3})^\dagger$
$10^3 \mathcal{B}_{\Xi^0 \eta}$	$1.7^{+1.0}_{-1.7}$			$10^2 \mathcal{B}_{\Sigma^+ \eta'}$	$1.0^{+1.6}_{-0.8}$
$10^3 \mathcal{B}_{\Xi^0 \eta'}$	$8.6^{+11.0}_{-6.3}$			$10^2 \mathcal{B}_{\Xi^0 K^+}$	$(0.5 \pm 0.1)^\dagger$
$10^3 \mathcal{B}_{\Xi^- \pi^+}$	$15.7 \pm 0.7$			$10^2 \mathcal{B}_{\rho K^0}$	$(3.3 \pm 0.2)^\dagger$
$10^3 \mathcal{B}_{\Lambda^0 \bar{K}^0}$	$8.3 \pm 0.9$			$10^2 \mathcal{B}_{\rho \pi^+}$	$(1.3 \pm 0.2)^\dagger$
$10^4 \mathcal{B}_{\Sigma^+ \pi^-}$	$2.0 \pm 0.5$	$10^4 \mathcal{B}_{\Sigma^+ \pi^+}$	$18.5 \pm 2.2$	$10^4 \mathcal{B}_{\Sigma^0 K^0}$	$8.0 \pm 1.6$
$10^4 \mathcal{B}_{\Sigma^+ \pi^+}$	$9.0 \pm 0.4$	$10^4 \mathcal{B}_{\Sigma^+ \pi^0}$	$18.5 \pm 2.2$	$10^4 \mathcal{B}_{\Sigma^0 K^+}$	$(4.0 \pm 0.8)^\dagger$
$10^4 \mathcal{B}_{\Sigma^0 \pi^0}$	$3.2 \pm 0.3$	$10^4 \mathcal{B}_{\Sigma^+ \eta}$	$28.4^{+8.2}_{-6.9}$	$10^4 \mathcal{B}_{\rho \pi^0}$	$5.7 \pm 1.5$
$10^4 \mathcal{B}_{\Sigma^0 \eta}$	$3.6^{+1.0}_{-0.9}$	$10^4 \mathcal{B}_{\Sigma^+ \eta'}$	$13.2^{+24.0}_{-11.9}$	$10^4 \mathcal{B}_{\rho \eta}$	$(12.5^{+3.8}_{-3.6})^\dagger$
$10^4 \mathcal{B}_{\Sigma^0 \eta'}$	$1.7^{+3.0}_{-1.5}$	$10^4 \mathcal{B}_{\Xi^0 K^+}$	$18.0 \pm 4.7$	$10^4 \mathcal{B}_{\rho \eta'}$	$12.2^{+14.3}_{-8.7}$
$10^4 \mathcal{B}_{\Xi^- K^+}$	$7.6 \pm 0.4$	$10^4 \mathcal{B}_{\rho \bar{K}^0}$	$20.3 \pm 4.2$	$10^4 \mathcal{B}_{\eta \pi^+}$	$11.3 \pm 2.9$
$10^4 \mathcal{B}_{\Xi^0 K^0}$	$6.3 \pm 1.2$	$10^4 \mathcal{B}_{\Lambda^0 \pi^+}$	$1.6 \pm 1.2$	$10^4 \mathcal{B}_{\Lambda^0 K^+}$	$(4.6 \pm 0.9)^\dagger$
$10^4 \mathcal{B}_{\rho K^-}$	$2.1 \pm 0.5$				
$10^4 \mathcal{B}_{n \bar{K}^0}$	$7.9 \pm 1.4$				
$10^4 \mathcal{B}_{\Lambda^0 \pi^0}$	$0.2 \pm 0.2$				
$10^4 \mathcal{B}_{\Lambda^0 \eta}$	$1.6^{+1.2}_{-0.8}$				
$10^4 \mathcal{B}_{\Lambda^0 \eta'}$	$9.4^{+11.6}_{-6.8}$				
$10^6 \mathcal{B}_{\rho \pi^-}$	$12.1 \pm 3.1$	$10^5 \mathcal{B}_{\Sigma^0 K^+}$	$8.8 \pm 0.4$	$10^6 \mathcal{B}_{\rho K^0}$	$12.2 \pm 6.0$
$10^6 \mathcal{B}_{\Sigma^- K^+}$	$44.5 \pm 2.1$	$10^5 \mathcal{B}_{\Sigma^- K^0}$	$17.6 \pm 0.8$	$10^6 \mathcal{B}_{n K^+}$	$12.2 \pm 6.0$
$10^6 \mathcal{B}_{\Sigma^0 K^0}$	$22.3 \pm 1.0$	$10^6 \mathcal{B}_{\rho \pi^0}$	$23.8 \pm 6.1$		
$10^6 \mathcal{B}_{\rho \pi^0}$	$6.0 \pm 1.5$	$10^5 \mathcal{B}_{\rho \eta}$	$10.5^{+4.5}_{-4.0}$		
$10^6 \mathcal{B}_{\rho \eta}$	$26.5^{+11.4}_{-10.1}$	$10^5 \mathcal{B}_{\rho \eta'}$	$12.1^{+10.7}_{-9.7}$		
$10^6 \mathcal{B}_{\rho \eta'}$	$30.7^{+42.3}_{-24.4}$	$10^6 \mathcal{B}_{\eta \pi^+}$	$47.6 \pm 12.2$		
$10^6 \mathcal{B}_{\Lambda^0 K^0}$	$14.4 \pm 3.7$	$10^6 \mathcal{B}_{\Lambda^0 K^+}$	$56.8 \pm 14.5$		

## Summary

- We find out

$$\mathcal{B}(\Xi_c^0 \rightarrow \Xi^- \pi^+) = (15.7 \pm 0.7) \times 10^{-3},$$

which is consistent with the experiment.

- Through the experimental data, we predict the non-leptonic decays branching ratios.

*THANKS FOR  
YOUR ATTENTION*

**HAPPY  
NEW YEAR  
2019**

